Algorithm: RWR_Cluster

Data: $ListofQuerySets \leftarrow \{Lists\,of\ \ sets\ of\ start\,Nodes\}$
$G \leftarrow Global\ PairWise\ BLAST\ BitScore\ Graph$

RWR Parameters:
$restart\_prob = probability\ of\ returning\ to\ the\ start\ nodes$
$threshold = repeat\ loop\ till\ L1\ error \leq threshold$
$iter\_cutoff = maximum\ number\ of\ iterations$
$K = Step\ size$
Permutation Statistics parameters:
$num\_replicates = number\ of\ replications$

Result: $ClusterMap$:
$Map(Query\_Name \rightarrow Map(Node \rightarrow Scores(Statistics)))$

begin
$Cluster\_Map \leftarrow Map(Query\_Name \rightarrow Map(Node \rightarrow Scores))$

Random Walk Section:
forall the $QuerieSet \in ListofQuerySets$
do
$Cluster\_Map \leftarrow RWR\ in\ threads(QuerySet, RWR\_Parameters)$
end

Permutation Statistics Section:
$Population \leftarrow Map(Query\_Name \rightarrow$
$Random\_Permutation(ListofQuerySets, RWRParameters, num\_replicates)$

Summarize Statistics Section:
forall the $QuerySet \in Keys(Cluster\_Map)$
do
$Cluster : Map(Node \rightarrow Scores) \leftarrow Cluster\_Map(QuerySet)$
forall the $c.member :\ members\ of\ ClusterofQuerySet$
do
$p.value \leftarrow \frac{|scores\ \ from\ \ Population(QuerySet) \geq Score|}{size\ of\ \ Population}$

$max.norm.score \leftarrow Score\ normalized\ by\ max\ score\ in\ Cluster$
$species.norm.score \leftarrow$
$Score\ normalized\ by\ max\ score\ within\ same\ species\ in\ Cluster$

Update scores of $Cluster$ with [score,p.value,norm.score,species.norm.score]
end

Update $Cluster\_Map$ with $Cluster$
end
end

Algorithm: *RWR_in_threads*

Data: $Queries \rightarrow \{Set\,of\,start\,Nodes\}$
Global variables:
$G \leftarrow Global\ PairWise\ BLAST\ BitScore\ Graph$
$threshold = repeat\ loop\ till\ L1\ error \leq threshold$
$iter\_cutoff = repeat\ loop\ at\ least\ iteration\ threshold\ times\ K = Step\ size$

Result: $PostProbMap = Map(s \rightarrow probability\,to\,end\,walk\,at\,s)$,
$s \in Nodes\,in\,G\,with\,non-zero\,post-probabilities$

begin

$LocalGraph \leftarrow K - Step\ Neighborhood\ of\ Queries\ in\ G$
$W = Adjacency\ matrix\ from\ LocalGraph$
$index\_name\_map = Map(index\ of\ W\ \rightarrow Query\_Name)$
$name\_index\_map = Map(Query\_Name \rightarrow index\ of\ W)$
$N = Number\ of\ Start\ Nodes$
$QIndices \rightarrow \{Set\ of\ indices\ of\ Queries\ in\ W\}$
$p^0 \leftarrow \left\{p_i^0\right\}\ \ for\ i \in indices\ of\ W$

$$p_i^0 = \begin{cases} \frac{1}{N}, & \text{if} i \in QIndices \\ 0, & \text{otherwise} \end{cases}$$

$normalize\ W$
while $|p^{t+1} - p^t| \leq threshold$ ***and*** $iter \leq iter\_cutoff$ **do**
  $p^{t+1} = (1-r)Wp^t + rp^0$
end
$pfinal = p^{t+1}$
$Create\ a\ post\ probability\ map\ from\ p^{final}$:
$PostProbMap = Map(s \rightarrow probability\,to\,end\,walk\,at\,s)$,
$s \in Nodes\,in\,LocalGraph\,with\,nonzero\,values\,in\,p^{t+1}$

Update Concurrent HashMap holding Results

end

Algorithm: Permutation_Statistics

Data: $ListofQuerySets \rightarrow \{Lists\,of\ query\,sets\}$
$Degree\_Node\ Map\ (d \rightarrow \{Set\,of\ Nodes\,with\ degree\ d\})$
Global variables:
$G \leftarrow Pairwise\ sequence\ similarity\ network$

Result: $Population\_Map$:
$Map(Query\_Name \rightarrow \{population\ of\ post\ probability\ values\}))$

Get Sample Populations for the QuerySets:
SampleSpace $\leftarrow Get\_SampleSpace\_for\_QuerySets$ Sets(ListofQuerySets)

Permutation Statistics Section:
$Population\_Map \leftarrow Post\ rwr\ probability\ values\ from\ permuted\ queries$

forall the $queryset \in ListofQuerySets$
do
  $q.size \leftarrow number\ of\ nodes\ in\ queryset\ q.name \leftarrow name\ of\ queryset$ **repeat**
    $Perm_Query \leftarrow$Randomly sample q.size nodes from SampleSpace[q.name]
    $Update\ Population\_n \leftarrow RWR\ in\ threads(Perm\_Query, RWR\_Parameters)$
    $rep++$
  until $rep \leq num\_replicates$;
  $Update:\ Population\_Map[n] \leftarrow Population\_n$
end

Algorithm: *Get_SampleSpace_for_QuerySets*

Data: $ListofQuerySets \rightarrow \{Lists\,of\ QuerySets\}$
$Degree\_Map\ (d \rightarrow \{Set\,of\ Nodes\,with\ degree\ d\ for\ G\})$

Result: $SampleSpace\_Map:\ Map(querysetid \rightarrow Set\ of\ Nodes)$

forall the $queryset \in ListofQuerySets$
do
$queryset.size \leftarrow number\ of\ nodes\ in\ queryset$
$max.degree \leftarrow max(degree(nodes\ in\ queryset))$
$min.degree \leftarrow min(degree(nodes\ in\ queryset))$

$SampeSpace \leftarrow \{Pooled\ sets\ of\ nodes\ from\ Degree\_Map[max.degree + range]\ to\ Degree\_Map[min.degree - range]\}$
$Add\ (querysetid \rightarrow SampleSpace)\ map\ to\ SampleSpace\_Map$
end